

Physical Principles in Biology  
Biology 3550  
Fall 2018

## Lecture 24

Thermodynamics: Expansion and Compression of a Gas

Friday, 26 October

©David P. Goldenberg  
University of Utah  
goldenberg@biology.utah.edu

# Why is Thermodynamics Important?

- Thermodynamics is the fundamental science of energy, something almost everyone cares about! (because they pay for it)
- Defines the rules for interchange of different forms of energy. (e.g., the conversion of an  $H^+$  concentration gradient into mechanical motion in the bacterial rotary motor.)
- Places strict constraints on whether or not a physical, chemical or biological process is favorable under specified conditions.  
But, it won't say whether the process will take place or how fast!
- Particularly important in the context of climate change and society's need for energy.

# Why is Thermodynamics Hard?

- The ideas are abstract and subtle.
- It depends on math! (And, the quantities are subtle.)
- The language can be confusing (and varies among disciplines).
- Historical confusion.
  - Developed over multiple generations of scientists in the 18<sup>th</sup>–20<sup>th</sup> centuries.
  - Periods of profound confusion.
- But it's worth it!

# Units of Energy

- Energy is the ability to do work.
- Unit of work or energy:  $1 \text{ J} = 1 \text{ N} \cdot \text{m} = 1 \text{ Kg} \cdot \text{m}^2/\text{s}^2$   
Energy required to apply 1 N of force over a distance of 1 m.  
 $1 \text{ J} = 1 \text{ watt} \cdot \text{s}, 1 \text{ kwatt} \cdot \text{hr} = 3.6 \times 10^6 \text{ J}$
- Another unit of energy commonly used in thermodynamics: calorie
  - Originally defined as energy required to raise the temperature of 1 g of water by  $1^\circ\text{C}$ . (depends on starting temperature)
  - Now defined as exactly 4.184 J
- “Big C” Calorie, or “kg calorie”:  $1 \text{ Calorie} = 1,000 \text{ calories}$ .
  - Energy required to raise the temperature of 1 kg of water by  $1^\circ\text{C}$ .
  - Big C Calorie is the one used for nutritional information.
- Calorie units are still commonly used in thermodynamics because they directly relate energy to temperature.

# Temperature Versus Heat

## ■ Temperature

- A property of matter, which we measure with a thermometer.
- Directly related to the kinetic energy of the molecules making up the matter.
- For an ideal gas,  $E_k = 3kT/2$   
Three degrees of translational freedom, in  $x$ -,  $y$ -, and  $z$ -direction.
- Non-ideal gasses, liquids and solids have additional motional modes and generally greater kinetic energy at a given temperature.

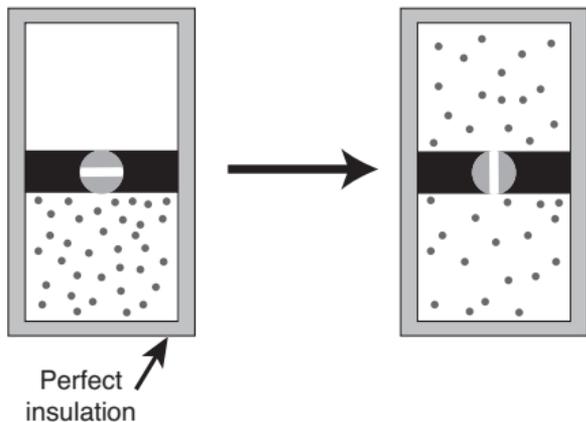
## ■ Heat

- Sometimes described as a “form of energy”, and it has the units of energy (joule or calorie).
- Better definition: Flow of energy from from a warmer object to a cooler one; equilibration of kinetic energy.
- At one time, heat was thought to be a massless substance, called “caloric”, that moved within or between objects.

# Our Starting Point for Thermodynamics: Expansion and Compression of Gasses

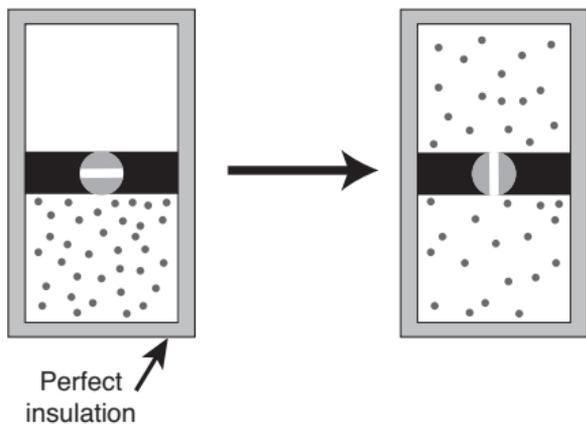
- Historical origins:
  - Development of thermodynamics was first motivated by the invention of the steam engine, and the desire to make better ones.
  - Many of the basic ideas were formulated in this context and are still easiest to visualize in it.
  - Original treatments did not consider molecular motion (because it wasn't understood) and were very abstract; “classical thermodynamics.”
  - Molecular interpretation developed later, “statistical thermodynamics”.
  - Classical and statistical thermodynamics are each self-sufficient and are consistent with one another.
- We will use both classical and statistical viewpoints, which complement each other.
- An ideal gas is the simplest system in which to formulate ideas.
- Also ties back to our discussion of molecular motion in diffusion.

# Adiabatic (without heat flow) Expansion of a Gas



- Insulation prevents heat flow into or out of device.
- What changes?

# Clicker Question #1

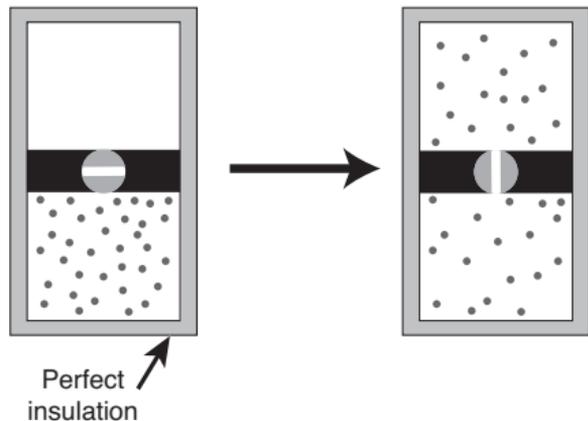


Which of the following properties of the gas change?

- A) Temperature
- B) Pressure
- C) Volume
- D) Kinetic energy

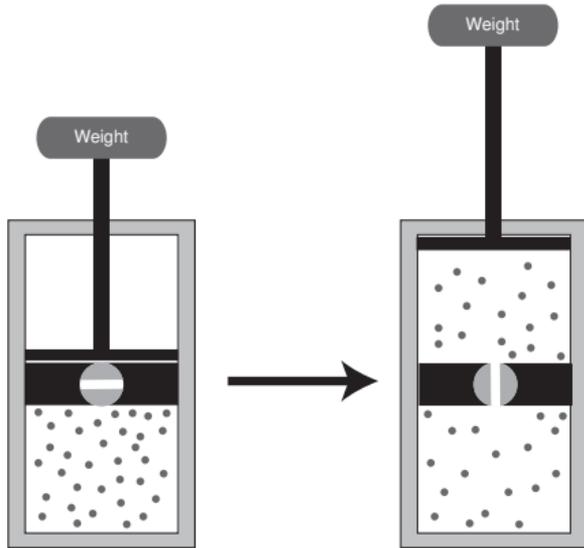
Any answers count for now!

# Adiabatic (without heat flow) Expansion of a Gas



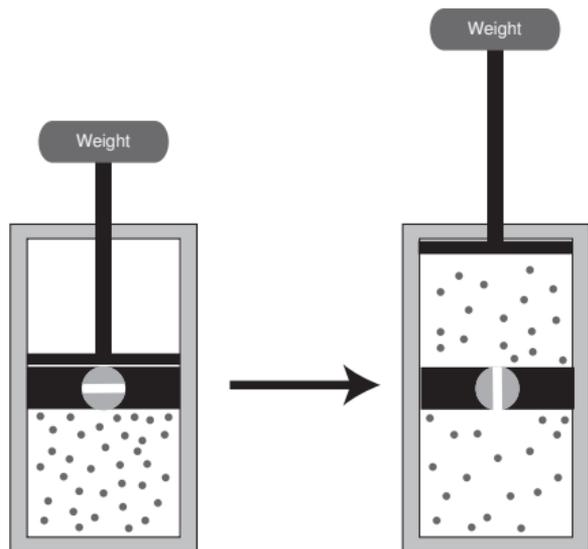
- Insulation prevents heat flow into or out of device.
  - Temperature stays constant.
- What changes?
  - Volume of gas increases.
  - Pressure of gas decreases ( $PV = nRT$ )
  - Does the energy stay constant? (yes)
  - Has any work been done? (no)
  - Has anything else changed?

# Adiabatic Gas Expansion With Work



- Collisions of gas molecules with piston move the weight up.
- What changes?

## Clicker Question #2

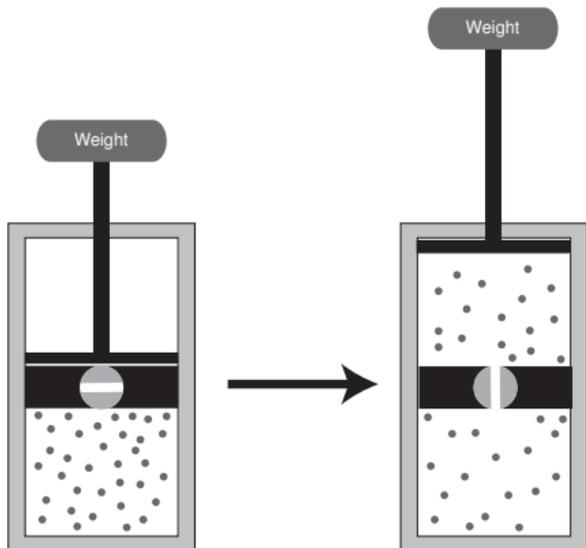


Which of the following properties of the gas change?

- A) Temperature
- B) Pressure
- C) Volume
- D) Energy

Any answers count for now!

# Adiabatic Gas Expansion With Work



- Collisions of gas molecules with piston move the weight up.
- What changes?
  - Volume of gas? (increases)
  - Temperature? (decreases as energy is transferred to piston.)
  - Pressure? (decreases, more than without the weight)
  - Energy?  
Has any work been done?  
(yes)
  - Where did the energy to do the work come from?  
Gas molecules have lost kinetic energy.

# Rules for Keeping Score

- Change in energy of the gas molecules (the “system”):

$$\Delta E = E_{\text{final}} - E_{\text{start}}$$

- Work,  $w$ :

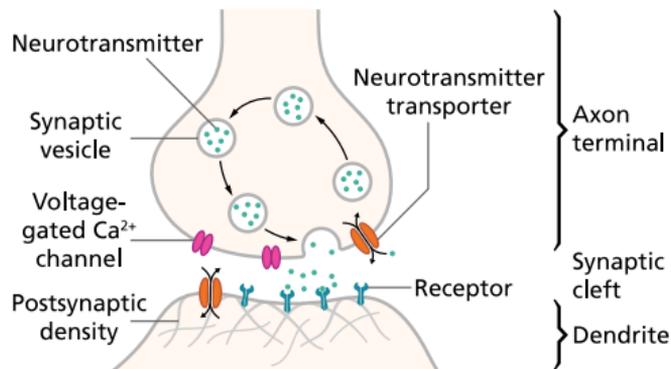
- $w > 0$ , when work is done on the system.
- $w < 0$ , when the system does work on the outside world, as in the expansion of the gas.

- For the adiabatic expansion of a gas with work:

- $E_{\text{final}} < E_{\text{start}}$ , and  $\Delta E < 0$
- $w < 0$ , because the system did work.
- $\Delta E = w$ : Where else could the energy come from?
- Does  $\Delta E$  always equal  $w$ ?

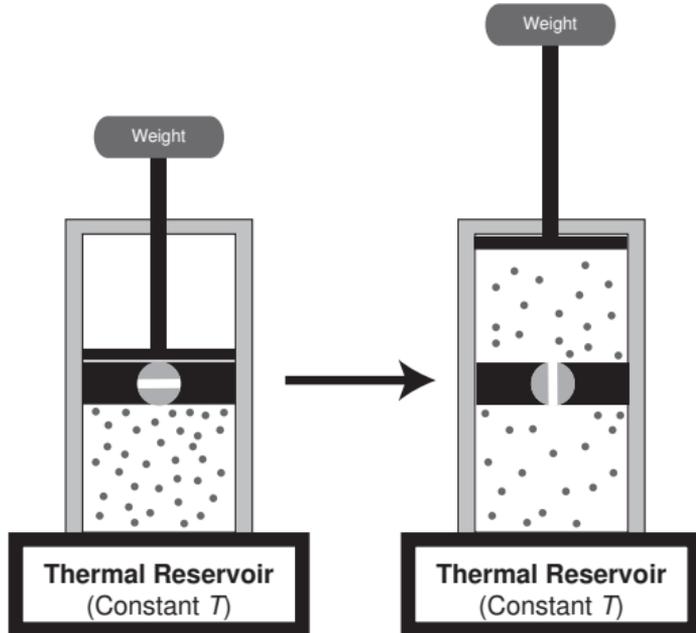
- Some books use the opposite sign convention for  $w$ .

# What Does This Have to Do with Biology?



- Dilution of molecules in solution is analogous to expansion of a gas.
- How much work (energy) is required to package neurotransmitters into vesicles?
- How much energy is lost when neurotransmitters are released into a synapse?
- Other examples of dilution and concentration in biology?

# Isothermal Expansion with Work



- Reservoir keeps the gas temperature constant. (isothermal)
- What changes?